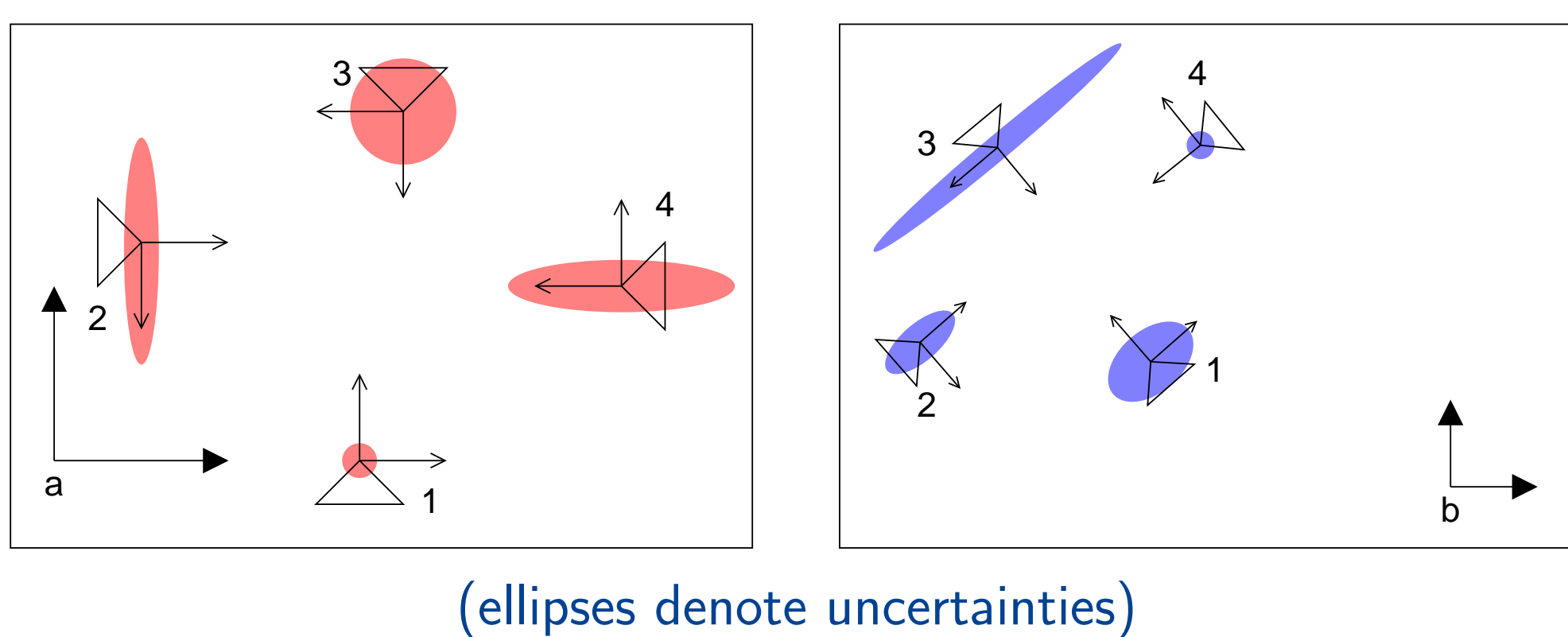


## Motivation

- In classical photogrammetry, evaluations of bundle adjustments are based on 3D points
- Automatic methods yield 2 problems for the evaluation:
  1. The choice of points differs for each method
  2. Methods often contain random components (i.e. RANSAC)
- Following Pennec and Thirion (1995), we conclude:
  1. Use the orientation parameters for benchmarking
  2. Benchmark against a reference dataset

## Overview of the benchmarking approach

Given 2 sets of corresponding orientation parameters in arbitrary coordinate systems  $\{^a\mathbf{d}_1, {}^a\Sigma_{d_1d_1}\}$  and  $\{^b\mathbf{d}_2, {}^b\Sigma_{d_2d_2}\}$



Derive the following measures:

- **consistency**  $c$  of form deviation and internal precision
- **precision level**  $p$  related to a reference dataset

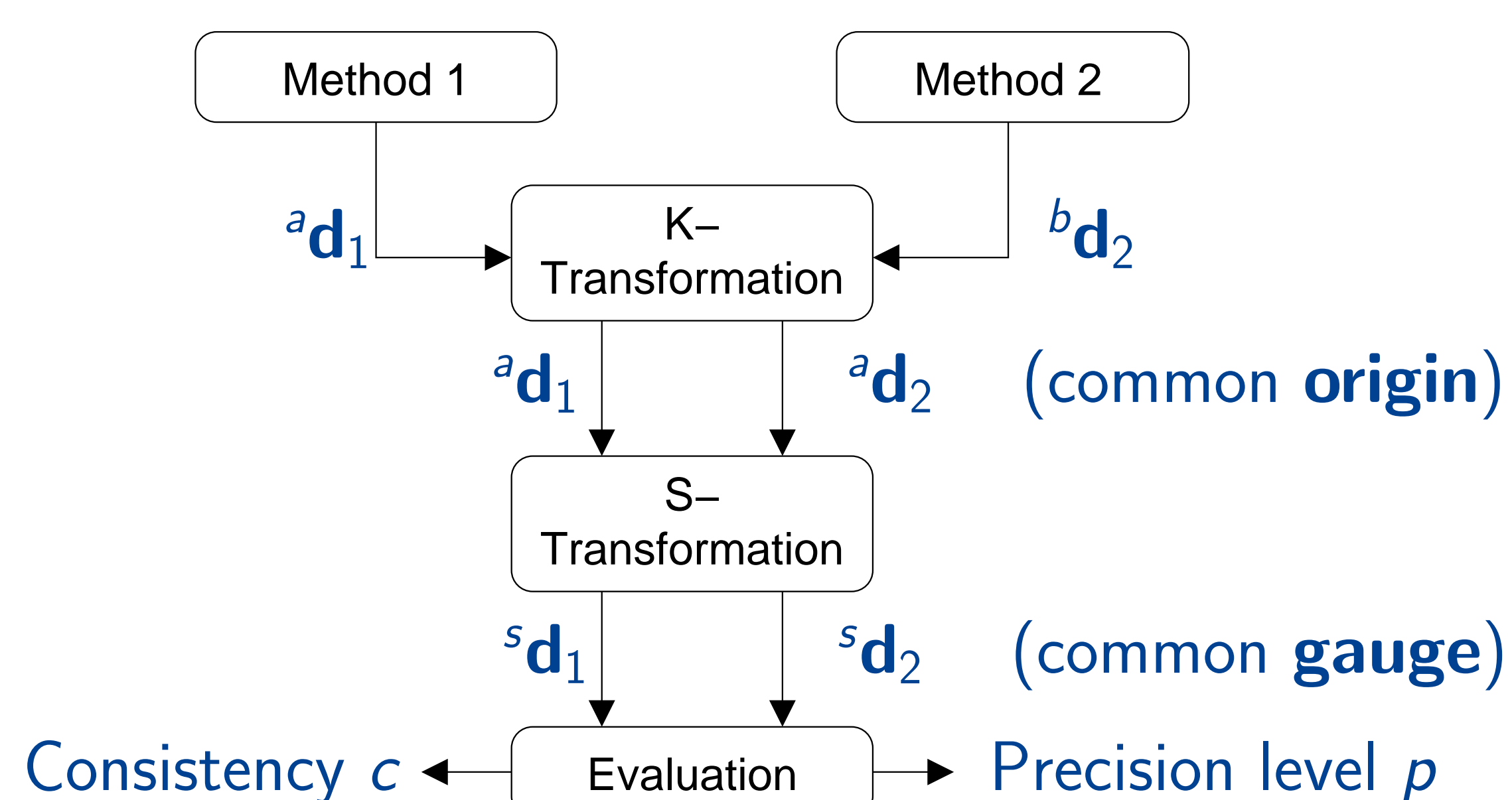
For methods with random components also derive

- the **sample consistency**  $c_s$  over repeated estimates

**Benchmark test:** For  $2 \leq i \leq M$  methods, compute all three measures. Require a valid range of  $c_{s_i}$ , then report  $c_i$  and  $p_i$  w. r. t. the same reference dataset.

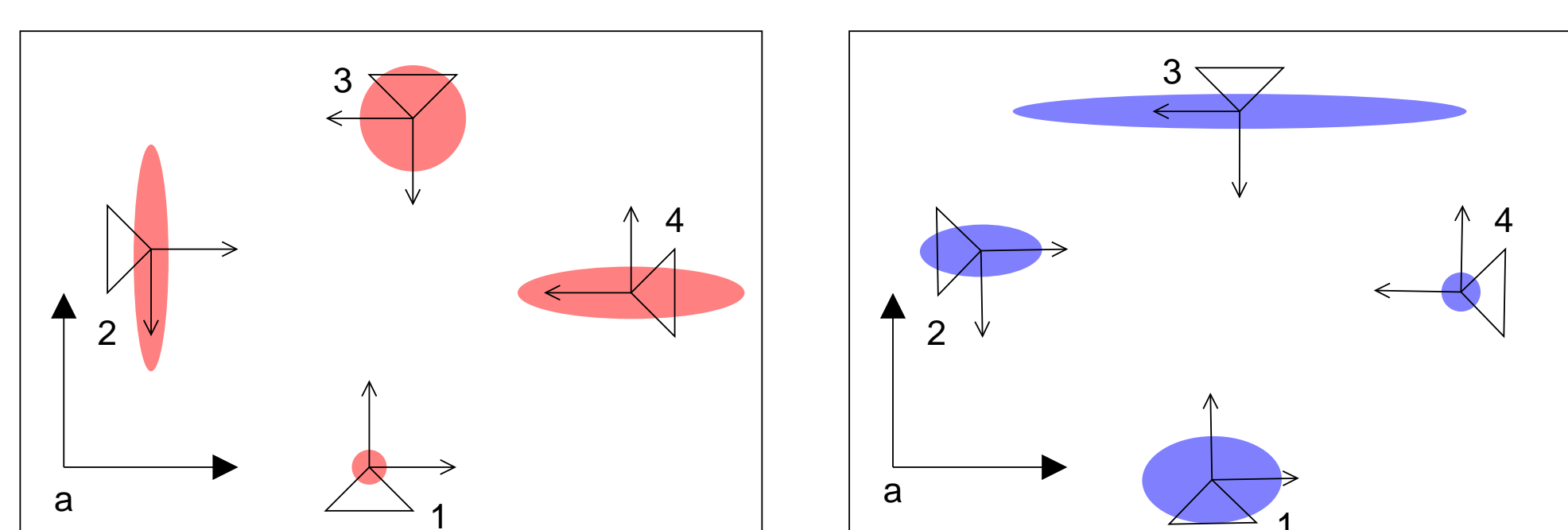
## Parameter transformations

- **Gauge problem:** For comparison, the datasets have to be transformed to a well-defined coordinate system  $s$ .
- **Solution:** Derive K- and S-transformations (Baarda, 1967; Molenaar, 1981) for sets of orientation parameters



### (1) K-transformation

- Estimate a similarity transformation  $K(\mathbf{t}_K, \mathbf{q}_K, \lambda_K)$  between  $^a\mathbf{d}_1$  and  $^b\mathbf{d}_2$  that brings  $^b\mathbf{d}_2$  into system  $a$
- Update  $^b\Sigma_{d_2d_2}$  using linear error propagation. Observe from the ellipses that **the gauge still differs!**



### (2) S-transformation

- A differential non-stochastic similarity transformation into a well-defined coordinate system  $s$

$$^s\mathbf{d}_{in} = \Delta S \circ ^a\mathbf{d}_{in} \quad i = \{1, 2\}$$

- Define weight matrix  $W_s$  and use

$$^sS = I - A(A^T W_s A)^{-1} A^T W_s$$

to obtain the S-transformation for both datasets

$$^s\mathbf{d}_i = ^sS \circ ^a\mathbf{d}_i \quad ^s\Sigma_{d_id_i} = ^sS \circ ^a\Sigma_{d_id_i} \circ ^sS^T \quad i = \{1, 2\}$$

- The Jacobian  $A$  is derived in Dickscheid et al. (2008)
- $^s\mathbf{d}_1$  and  $^s\mathbf{d}_2$  share the same gauge now

## Consistency $c$

- Interpretation: Form deviation of corresponding orientation parameters w. r. t. their internal precision.
- $c$  is based on the Mahalanobis distance:

$$c^2 = \frac{|^s\mathbf{d}_1 - ^s\mathbf{d}_2|_{(^s\Sigma_{d_1d_1} + ^s\Sigma_{d_2d_2})}}{R} \sim F_{R,\infty}$$

assuming  $^s\Sigma_{d_1d_1}, ^s\Sigma_{d_2d_2}$  uncorrelated, with  $R \hat{=} \text{dof}$ .

## Precision level $p$

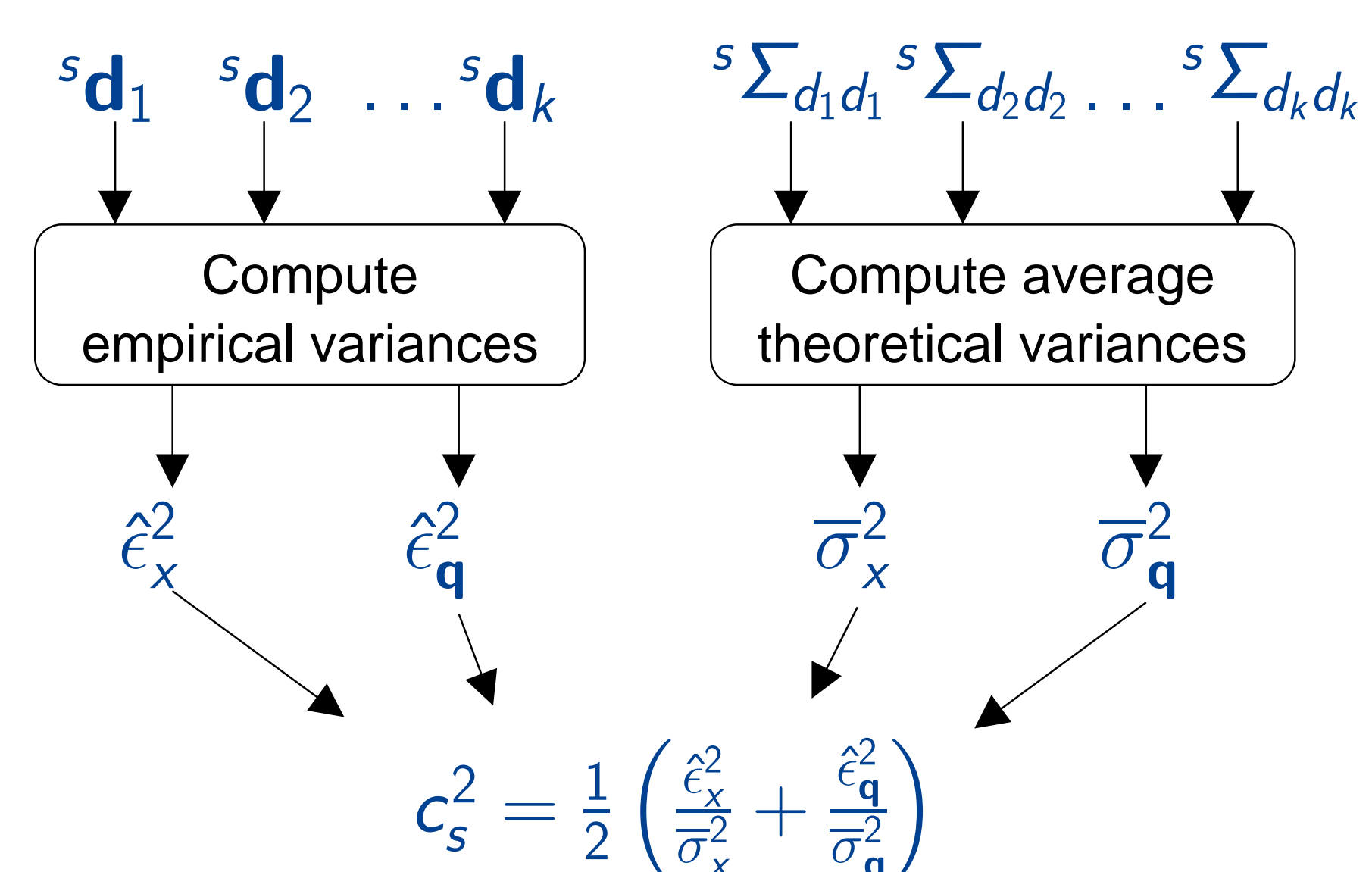
- Interpretation: Distance between two covariance matrices, based on Förstner and Moonen (1999)
- $p$  is derived by computing the generalized eigenvalues  $r^2$  from  $|^s\Sigma_{d_1d_1} - r^2 \cdot ^s\Sigma_{d_2d_2}| = 0$  to get

$$p := e^{\sqrt{\ln r^2}} \geq 1$$

- $p$  is the average quadratic deviation of the ratio of standard deviations from 1.

## Sample consistency $c_s$

- Interpretation: Consistency of the variation in orientation parameters w. r. t. their average internal precision
- Compute  $K$  repeated estimates under identical conditions, i. e. yielding  $K$  sets  $\{^a\mathbf{d}_k, {}^a\Sigma_{d_kd_k}\}$
- Again,  $c_s$  is derived after applying the K- and S-transformation on all  $K$  sets



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