# Endoscopic Video Manifolds

Atasoy S.<sup>1,2</sup>, Mateus D.<sup>1</sup>, Lallemand J.<sup>1</sup>, Meining A.<sup>1</sup>, Yang G.Z.<sup>2</sup> and Navab N.<sup>1</sup> Technical University of Munich<sup>1</sup>, Imperial College London<sup>2</sup> {atasoy, mateus, lalleman, navab}@in.tum.de, {catasoy, g.z.yang}@imperial.ac.uk



### Abstract

In this work, we address two tasks: clustering of poor-quality frames and different scenes in endoscopic videos. For each task, our method creates a manifold representation using an appropriate inter-frame similarity measure and then performs a clustering on the created endoscopic video manifolds (EVMs). The introduced EVMs enable the clustering of poor-quality frames and grouping of different segments of the endoscopic video in an unsupervised manner. Furthermore, we present two novel inter-frame similarity measures for manifold learning to create structured manifolds from complex endoscopic videos.

# Problem Statement

- An endoscopic video  $\mathcal{I}$  can be represented by the set of its n individual frames  $\{\mathcal{I}_1, \mathcal{I}_2, \cdots, \mathcal{I}_n\}$ .
- Each frame is a data point in the high dimensional input space  $\mathcal{I}_1, \mathcal{I}_2, \dots \mathcal{I}_n \in \mathbb{R}^{w \times h}$ , where w and h are the width and height of the frames, respectively. Thus, the number of degrees of freedom (DoF) is equal to  $w \times h$ .
- Due to the continuity of the video sequence the actual DoF is much smaller. So, the high dimensional data points actually lie on a lower dimensional manifold  $\mathcal{I}_1, \mathcal{I}_2, \cdots, \mathcal{I}_n \in \mathcal{M}$ , where  $\mathcal{M}$  is a manifold embedded in  $\mathbb{R}^{w \times h}$ .

We propose to represent the endoscopic video by this embedded low dimensional manifold and perform the two tasks of clustering poor-quality frames and endoscopic scenes on the introduced EVMs.

## Methods

**Defining the similarities:** For each pair  $(\mathcal{I}_i, \mathcal{I}_j)$ , of the given n data points  $i, j \in \{1, \dots, n\}$ , first a similarity measure is defined  $W : \mathcal{I} \times \mathcal{I} \to \mathbb{R}$ .

Computing the adjacency graph: Given the similarity matrix W, first, k-nearest neighbours of each data point are computed. Then, the adjacency graph is created as:

$$A(i,j) = \begin{cases} 1 & \text{if } i \in \mathcal{N}_j^k \\ 0 & \text{otherwise,} \end{cases}$$
 (1)

where  $\mathcal{N}_{j}^{k}$  states the k-nearest neighbours of the j-th data point.

Learning the manifold: The intrinsic low dimensional sstructure is learned using the Laplacian Eigenmaps (LE) method [1].

Clustering on the manifold: Finally, the clustering is using the K-means algorithm [2].

## Inter-frame Similarities

1. Clustering Poor-Quality Frames: For this task, EVM is created using the following similarity measure:

$$W_{\text{EH}}(\mathcal{I}_i, \mathcal{I}_j) = 1 - \frac{acos\left(\langle (\mathcal{F}_i, \mathcal{F}_j)\rangle\right)}{||\mathcal{F}_i|| \cdot ||\mathcal{F}_j||},$$
(2)

where  $\mathcal{F}_i$  states the rotation invariant energy histogram computed from the power spectrum of frame  $\mathcal{I}_i$ .

2. Clustering Endoscopic Scenes:
For this task we propose two different similarity measures:

$$W_{\text{DOFF}}(\mathcal{I}_i, \mathcal{I}_j) = 1 - \frac{\psi_i^j}{\max(\psi_i^j)},$$

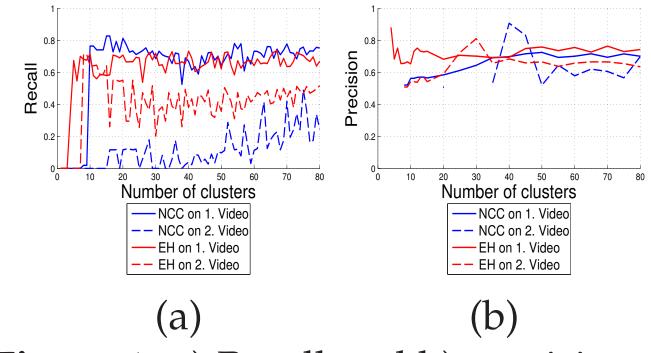
$$\psi_i^j = \sum_{x=1}^w \sum_{y=1}^h |\nabla \Phi_i^j(x, y)|,$$
(3)

where  $\Phi_i^j(x, y)$  states the optical flow from frame  $\mathcal{I}_i$  to frame  $\mathcal{I}_j$  and,

$$W_{NCC}(\mathcal{I}_i, \mathcal{I}_j) = NCC(\mathcal{I}_i, \mathcal{I}_j)$$
 (4)

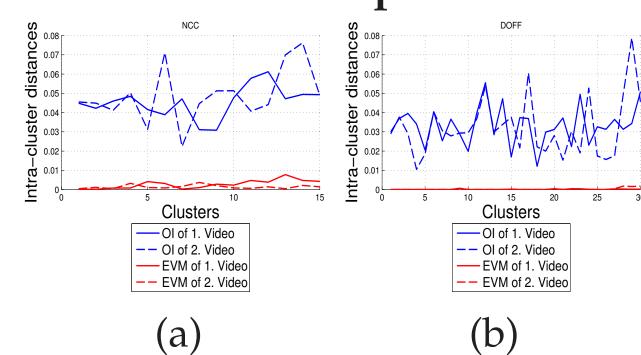
# Experiments

#### **Clustering Poor-Quality Frames:**



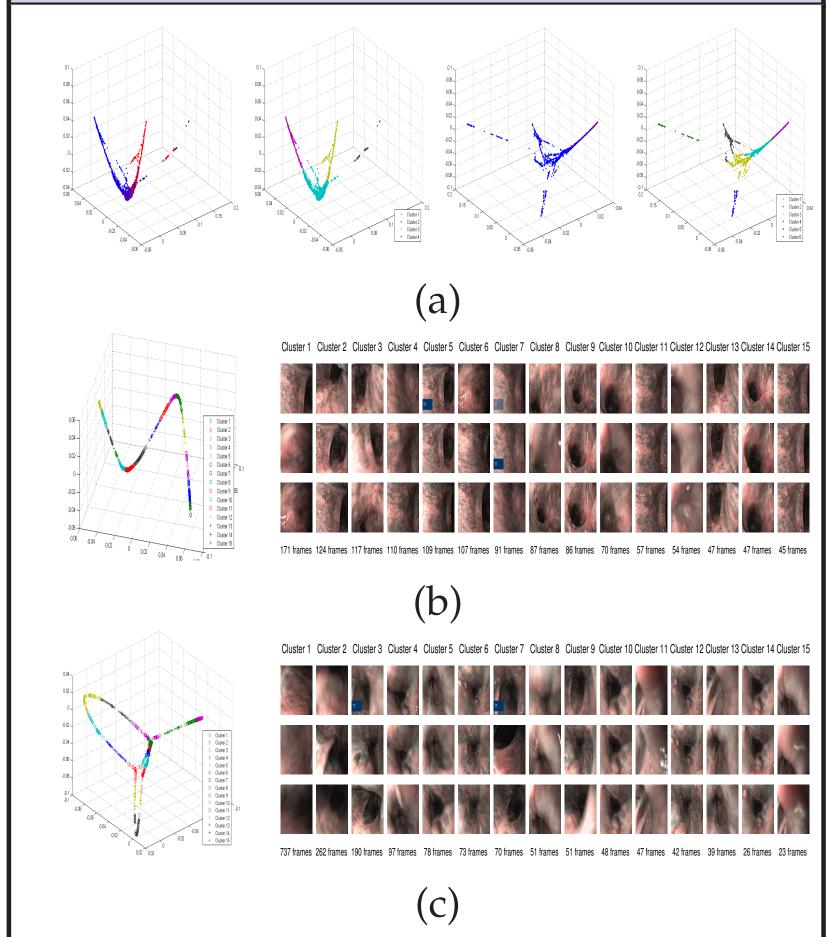
**Figure 1:** a) Recall and b) precision values for clustering uninformative frames.

#### Clusterin Endoscopic Scenes:



**Figure 2:** Intra-cluster distances for clustering endoscopic scenes. a)  $W_{\rm NCC}$  and b)  $W_{\rm DOFF}$ .

# Results



**Figure 3:** Clustering of (a) poor-quality frames using  $W_{\rm EH}$  and (b-c) endoscopic scenes using  $W_{\rm DOFF}$  and  $W_{\rm NCC}$ , respectively.

#### References

- [1] M. Belkin, P. Niyogi, Laplacian eigenmaps for dimensionality reduction and data representation. Neural computation, (2003)
- [2] J. Hartigan, M. Wong, A k-means clustering algorithm. JR Stat. Soc., (1979)