# NON-PARAMETRIC SUB-PIXEL LOCAL PSF ESTIMATION



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## Overview

- We prove formally that the non-parametric sub-pixel point spread function (PSF) estimation problem is well-posed with a single well chosen observation.
- Near-optimal accuracy achieved with a Bernoulli(0.5) noise calibration pattern.
- Local PSF estimated by solving a well conditioned linear system that does not require regularizers.
- Relative estimation error of 2% to 5%.
- Such a regularization and model free subpixel PSF estimation scheme is the first of its kind, to our knowledge.

# Motivation

Image blur can be a consequence of:

- Camera misusing or scene configuration
  - Wrongly setting the camera focus
  - Only an specific interval of depths in focus
  - Camera shake
  - Scene motion
- Physical camera phenomena
  - Light diffraction
  - Sensor averaging
  - Lens aberrations
  - Optical anti-aliasing filter

#### Our Goal

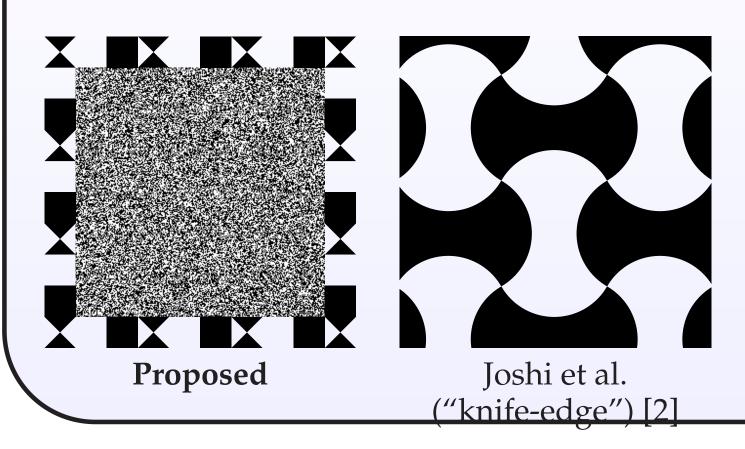
Accurately estimate a function, called point spread function -PSF, that models the blur due to intrinsic camera phenomena. Image ideally obtained from a null-area point light source (impulse response).

#### **Difficulties**

Most medium to high quality digital cameras (DSLR) acquire images at a spatial rate which is below the ideal Nyquist rate. Only aliased versions of the cameral point-spread function (PSF) can be directly observed.

# Our Approach

- Non-parametric non-blind local subpixel PSF estimation.
- Noise target specially designed for PSF estimation. (local blur information)



## Mathematical Formulation

- Solve inverse problem
- Extremely weak a priori assumption: small spatial support of the PSF. No regularization term needs to be added to the forward problem.
- Estimate h: samples of h at a rate  $\delta \times$  higher than the camera sampling (e.g  $4 \times$ )

Choose h to minimize the functional:

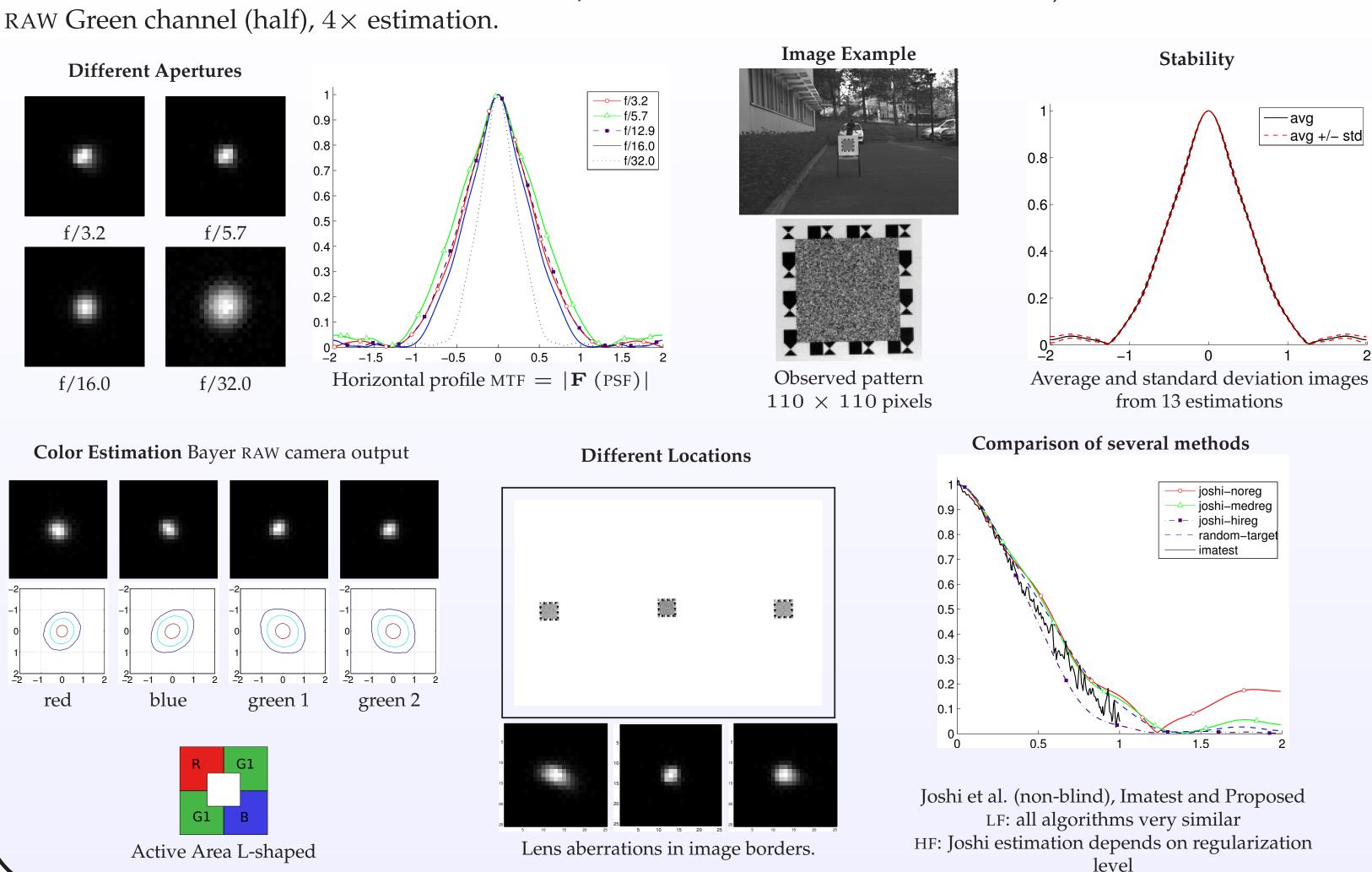
$$\underset{\mathbf{h}}{\operatorname{arg\,min}} \|\mathcal{S}_{\delta} \left( \tilde{\mathbf{u}}_{D} * \mathbf{h} \right) - \mathbf{v} \|^{2} \quad \text{s.t. } \mathbf{h} \geq 0$$

- $\tilde{\mathbf{u}}_D$  HR sharp distorted pattern image
- $\mathbf{v}$  blurred LR observed image (1 $\times$ ).
- h discrete HR PSF can be spatial variant (strictly not a convolution).
- $\mathcal{S}_{\delta}$  : Subsampling operator: takes HR and generates LR

#### Algorithm Description Kernel resolution size Geometric **Pattern** sx PSF **Captured Feature Transformation** sx PSF **Image Detection** Rasterization **Estimation Estimation** Illumination Captured Image Normalization **Estimation**

# Results: Real camera examples

Canon EOS 400D - Tamron AF 17-50mm F/2.8 XR Di-II lens. Taken at 100 ISO, 50mm RAW Green channel (half). 4 × estimation



#### DEMO & References

#### **Test it online** IPOL: Image Processing On Line

http://www.ipol.im/pub/algo/admm\_non\_blind\_psf\_estimation/

- [1] Delbracio M., Musé P., Almansa A., Morel JM. The non-parametric sub-pixel local point spread function estimation is a well posed problem, to appear in *IJCV*, 2011
- [2] Joshi N., Szeliski R., Kriegman DJ. PSF estimation using sharp edge prediction. in CVPR, 2008